

Thermodynamics: An Engineering Approach, 6th Edition
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Chapter (5)

MASS & ENERGY ANALYSIS OF A CONTROL VOLUMES

SOLVED PROBLEMS

Conservation of Mass

$$\dot{m}_1 = \dot{m}_2$$

$$\rho_1 A_1 V_1 = \rho_2 A_2 V_2$$

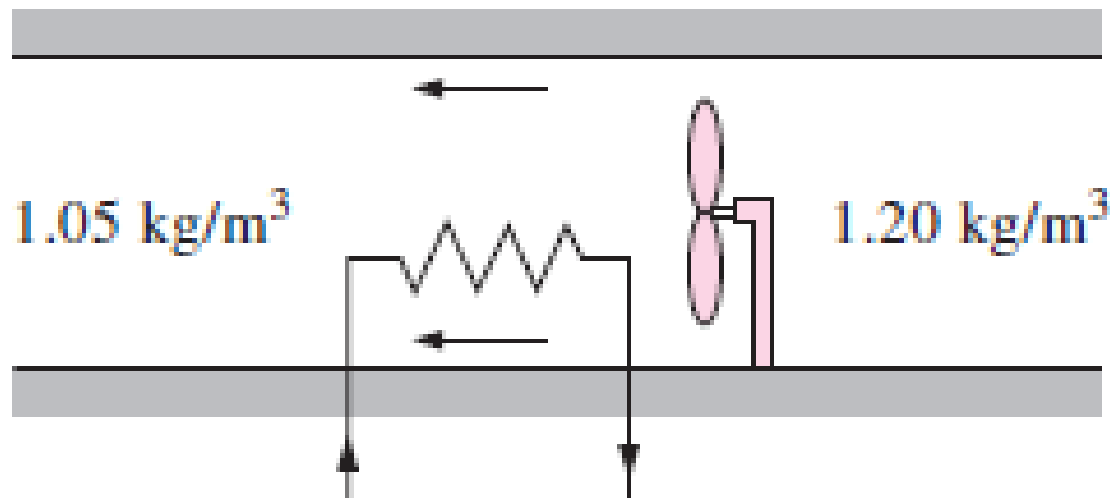
Problem (1-C)

5-1C Name four physical quantities that are conserved and two quantities that are not conserved during a process.

5-1C Mass, energy, momentum, and electric charge are conserved, and volume and entropy are not conserved during a process.

Problem (5-9C)

A hair dryer is basically a duct of constant diameter in which a few layers of electric resistors are placed. A small fan pulls the air in and forces it through the resistors where it is heated. If the density of air is 1.20 kg/m^3 at the inlet and 1.05 kg/m^3 at the exit, determine the percent increase in the velocity of air as it flows through the dryer.



Problem (5-9C)

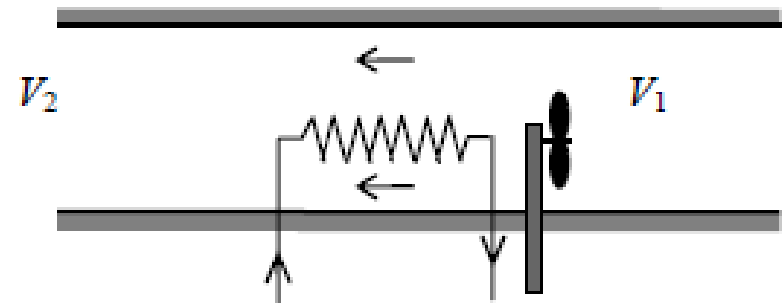
Assumptions Flow through the nozzle is steady.

Properties The density of air is given to be 1.20 kg/m^3 at the inlet, and 1.05 kg/m^3 at the exit.

Analysis There is only one inlet and one exit, and thus $\dot{m}_1 = \dot{m}_2 = \dot{m}$. Then,

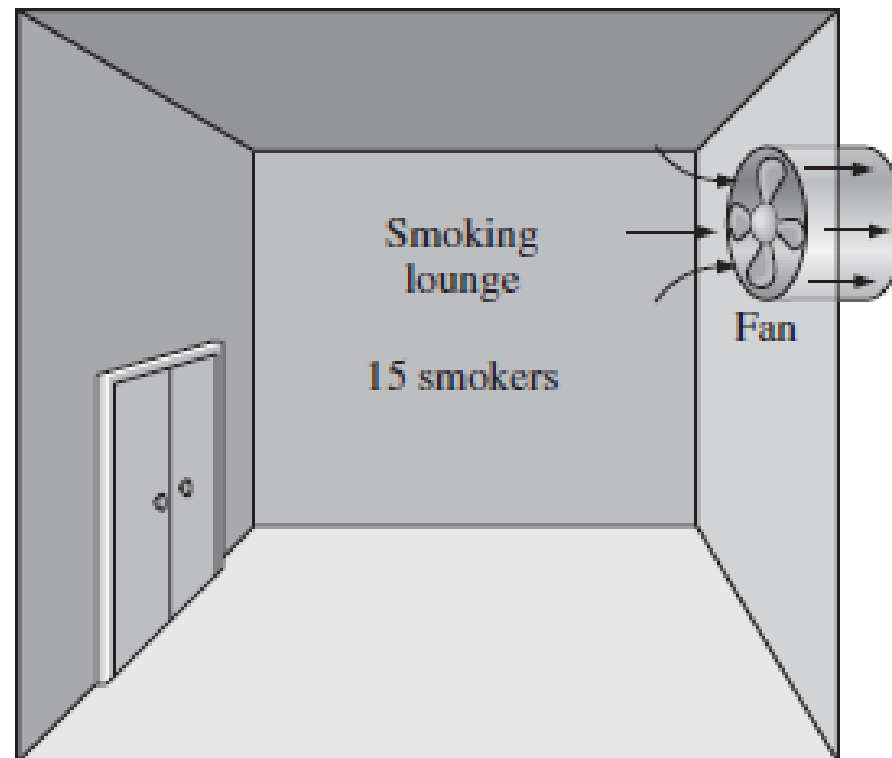
$$\begin{aligned}\dot{m}_1 &= \dot{m}_2 \\ \rho_1 AV_1 &= \rho_2 AV_2 \\ \frac{V_2}{V_1} &= \frac{\rho_1}{\rho_2} = \frac{1.20 \text{ kg/m}^3}{1.05 \text{ kg/m}^3} = 1.14 \quad (\text{or, an increase of } \mathbf{14\%})\end{aligned}$$

Therefore, the air velocity increases 14% as it flows through the hair drier.



Problem (5-11C)

A smoking lounge is to accommodate 15 heavy smokers. The minimum fresh air requirement for smoking lounges is specified to be 30 L/s per person (ASHRAE, Standard 62, 1989). Determine the minimum required flow rate of fresh air that needs to be supplied to the lounge, and the diameter of the duct if the air velocity is not to exceed 8 m/s.



Problem (5-11C)

Assumptions Infiltration of air into the smoking lounge is negligible.

Properties The minimum fresh air requirements for a smoking lounge is given to be 30 L/s per person.

Analysis The required minimum flow rate of air that needs to be supplied to the lounge is determined directly from

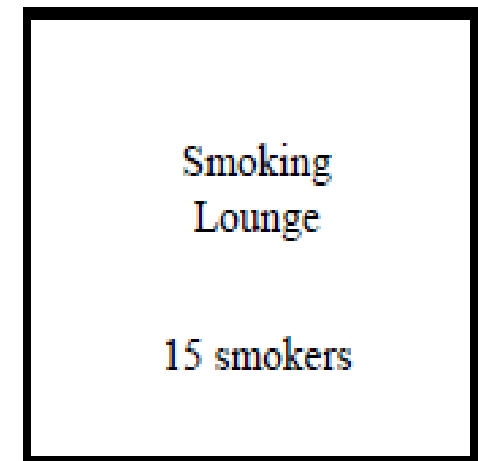
$$\begin{aligned}\dot{V}_{\text{air}} &= \dot{V}_{\text{air per person}} (\text{No. of persons}) \\ &= (30 \text{ L/s} \cdot \text{person})(15 \text{ persons}) = 450 \text{ L/s} = 0.45 \text{ m}^3/\text{s}\end{aligned}$$

The volume flow rate of fresh air can be expressed as

$$\dot{V} = VA = V(\pi D^2 / 4)$$

Solving for the diameter D and substituting,

$$D = \sqrt{\frac{4\dot{V}}{\pi V}} = \sqrt{\frac{4(0.45 \text{ m}^3/\text{s})}{\pi(8 \text{ m/s})}} = 0.268 \text{ m}$$



Therefore, the diameter of the fresh air duct should be at least 26.8 cm if the velocity of air is not to exceed 8 m/s.

Flow Work

$$W_{\text{flow}} = Pv \quad (\text{kJ/kg})$$

Problem (5-18C)

5-18C What are the different mechanisms for transferring energy to or from a control volume?

5-18C Energy can be transferred to or from a control volume as heat, various forms of work, and by mass.

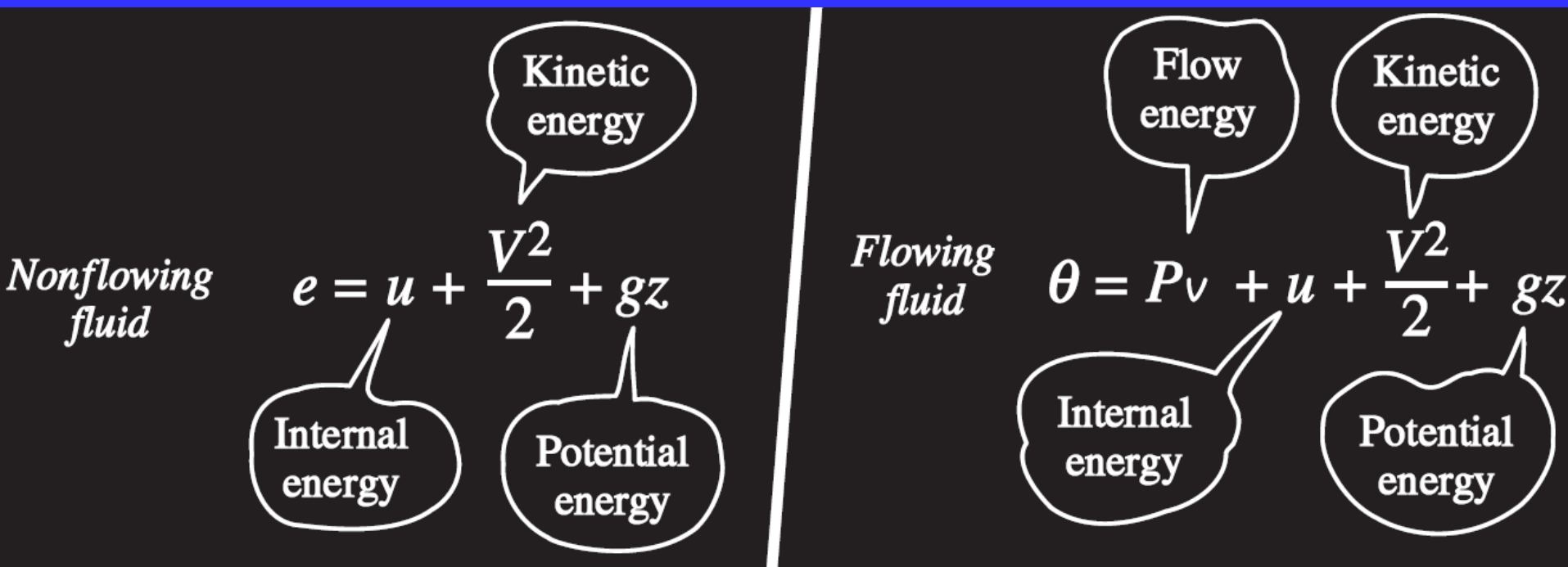
Problem (5-19C)

5-19C What is flow energy? Do fluids at rest possess any flow energy?

5-19C Flow energy or flow work is the energy needed to push a fluid into or out of a control volume. Fluids at rest do not possess any flow energy.

Problem (5-20C)

5-20C How do the energies of a flowing fluid and a fluid at rest compare? Name the specific forms of energy associated with each case.



Problem (5-23C)

5-23 A water pump increases water pressure. The flow work required by the pump is to be determined.

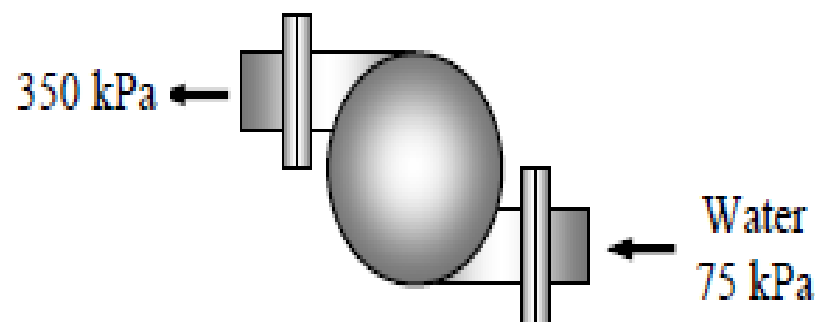
Assumptions 1 Flow through the pump is steady. 2 The state of water at the pump inlet is saturated liquid. 3 The specific volume remains constant.

Properties The specific volume of saturated liquid water at 75 kPa is

$$\nu = \nu_{f@75\text{kPa}} = 0.001037 \text{ m}^3/\text{kg} \quad (\text{Table A-5E})$$

Then the flow work relation gives

$$\begin{aligned} w_{\text{flow}} &= P_2 \nu_2 - P_1 \nu_1 = \nu(P_2 - P_1) \\ &= (0.001037 \text{ m}^3/\text{kg})(350 - 75)\text{kPa} \left(\frac{1 \text{ kJ}}{1 \text{ kPa} \cdot \text{m}^3} \right) \\ &= 0.285 \text{ kJ/kg} \end{aligned}$$



Nozzles & Diffusers

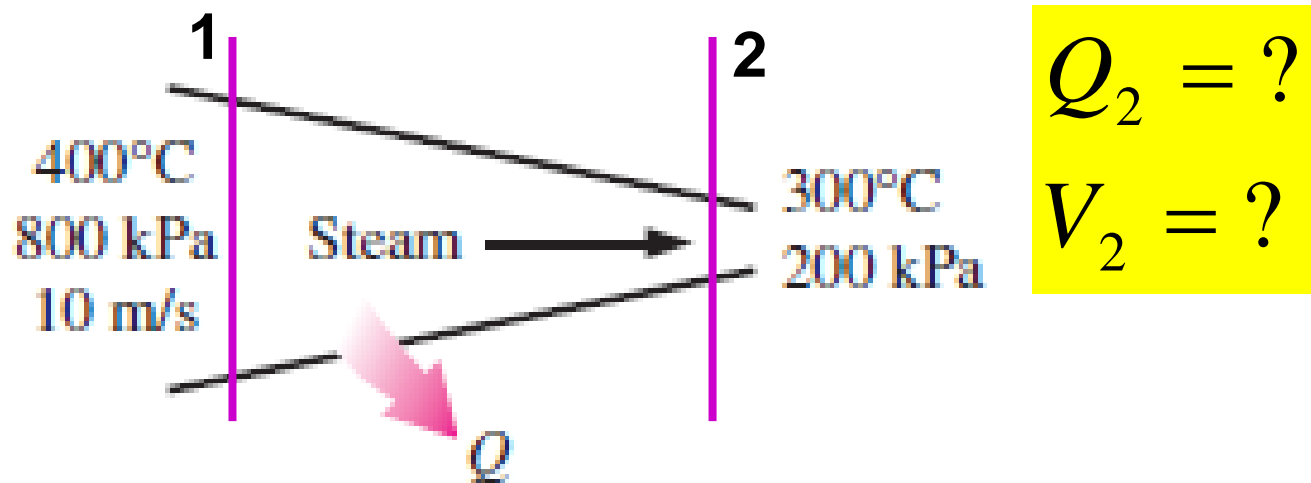
$$\dot{E}_{\text{in}} = \dot{E}_{\text{out}}$$

$$\dot{m} \left(h_1 + \frac{V_1^2}{2} \right) = \dot{m} \left(h_2 + \frac{V_2^2}{2} \right)$$

(since $\dot{Q} \cong 0$, $\dot{W} = 0$, and $\Delta p_e \cong 0$)

Problem (5-42C)

Steam enters a nozzle at 400°C and 800 kPa with a velocity of 10 m/s , and leaves at 300°C and 200 kPa while losing heat at a rate of 25 kW . For an inlet area of 800 cm^2 , determine the velocity and the volume flow rate of the steam at the nozzle exit. *Answers: 606 m/s , $2.74\text{ m}^3/\text{s}$*

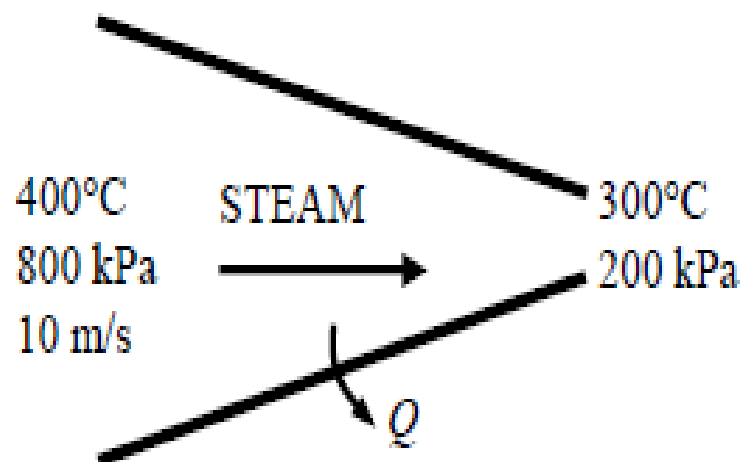


Problem (5-42C)

5-42 Heat is lost from the steam flowing in a nozzle. The velocity and the volume flow rate at the nozzle exit are to be determined.

Assumptions 1 This is a steady-flow process since there is no change with time. 2 Potential energy change is negligible. 3 There are no work interactions.

Analysis We take the steam as the system, which is a control volume since mass crosses the boundary. The energy balance for this steady-flow system can be expressed in the rate form as



Energy balance:

$$\underbrace{\dot{E}_{\text{in}} - \dot{E}_{\text{out}}}_{\text{Rate of net energy transfer by heat, work, and mass}} = \underbrace{\dot{\Delta E}_{\text{system}}}_{\text{Rate of change in internal, kinetic, potential, etc. energies}} \stackrel{\approx 0 \text{ (steady)}}{=} 0$$

$$\dot{E}_{\text{in}} = \dot{E}_{\text{out}}$$

Problem (5-42C)

$$\dot{E}_{\text{in}} = \dot{E}_{\text{out}}$$

$$\dot{m} \left(h_1 + \frac{V_1^2}{2} \right) = \dot{m} \left(h_2 + \frac{V_2^2}{2} \right) + \dot{Q}_{\text{out}} \quad \text{since } \dot{W} \cong \Delta pe \cong 0)$$

or

$$h_1 + \frac{V_1^2}{2} = h_2 + \frac{V_2^2}{2} + \frac{\dot{Q}_{\text{out}}}{\dot{m}}$$

The properties of steam at the inlet and exit are (Table A-6)

$$\left. \begin{array}{l} P_1 = 800 \text{ kPa} \\ T_1 = 400^\circ\text{C} \end{array} \right\} \begin{array}{l} v_1 = 0.38429 \text{ m}^3/\text{kg} \\ h_1 = 3267.7 \text{ kJ/kg} \end{array} \quad T_{\text{Sat},800\text{kPa}} = 170.41^\circ\text{C}$$

$$\left. \begin{array}{l} P_2 = 200 \text{ kPa} \\ T_2 = 300^\circ\text{C} \end{array} \right\} \begin{array}{l} v_2 = 1.31623 \text{ m}^3/\text{kg} \\ h_2 = 3072.1 \text{ kJ/kg} \end{array} \quad T_{\text{Sat},200\text{kPa}} = 120.21^\circ\text{C}$$

The mass flow rate of the steam is

$$\dot{m} = \frac{1}{v_1} A_1 V_1 = \frac{1}{0.38429 \text{ m}^3/\text{s}} (0.08 \text{ m}^2)(10 \text{ m/s}) = 2.082 \text{ kg/s}$$

Problem (5-42C)

Substituting,

$$3267.7 \text{ kJ/kg} + \frac{(10 \text{ m/s})^2}{2} \left(\frac{1 \text{ kJ/kg}}{1000 \text{ m}^2/\text{s}^2} \right) = 3072.1 \text{ kJ/kg} + \frac{V_2^2}{2} \left(\frac{1 \text{ kJ/kg}}{1000 \text{ m}^2/\text{s}^2} \right) + \frac{25 \text{ kJ/s}}{2.082 \text{ kg/s}}$$
$$\longrightarrow V_2 = \mathbf{606 \text{ m/s}}$$

The volume flow rate at the exit of the nozzle is

$$\dot{V}_2 = \dot{m} v_2 = (2.082 \text{ kg/s})(1.31623 \text{ m}^3/\text{kg}) = \mathbf{2.74 \text{ m}^3/\text{s}}$$

Compressors

$$\dot{E}_{in} = \dot{E}_{out}$$

$$\dot{W}_{in} + \dot{m}h_1 = \dot{m}h_2$$

Turbines

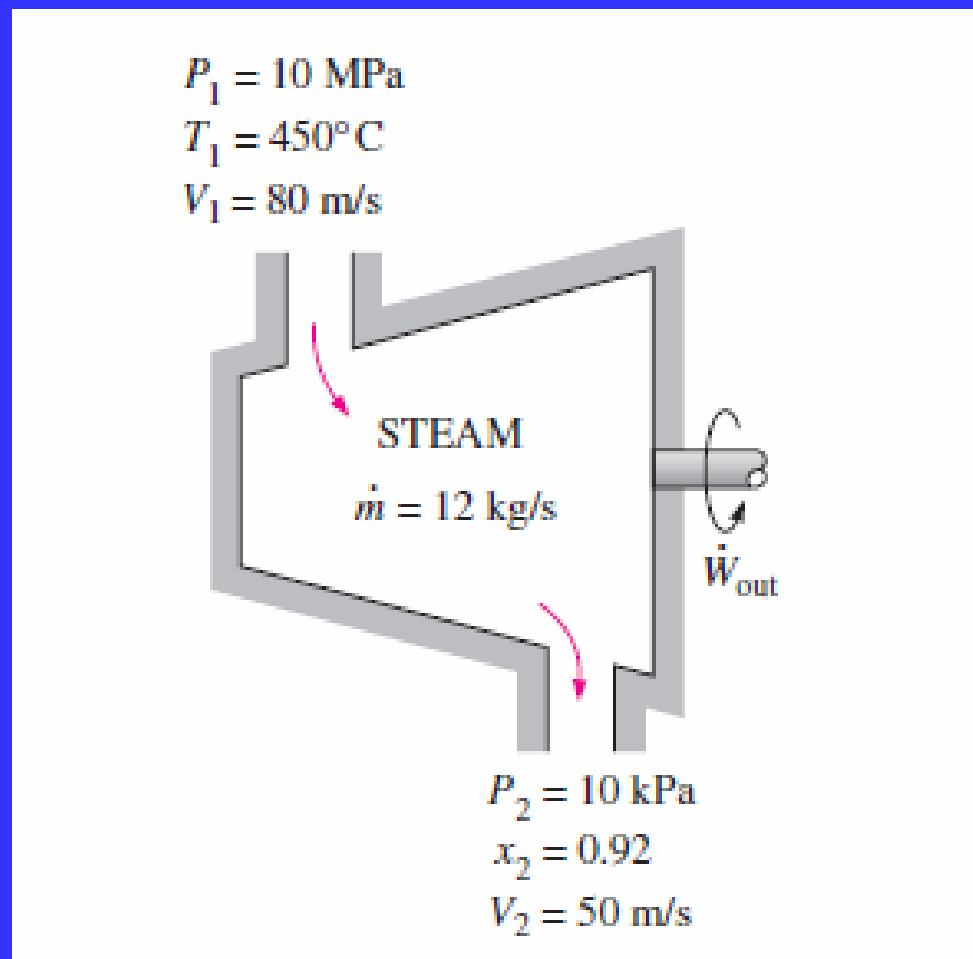
$$\dot{E}_{in} = \dot{E}_{out}$$

$$\dot{m}h_1 = \dot{W}_{out} + \dot{m}h_2$$

$$\dot{Q}_{in} = 0, \quad \dot{Q}_{out} = 0$$

$$\Delta KE = 0, \quad PE = 0$$

Problem (5-50C)



(a) the change in kinetic energy, (b) the power output, and (c) the turbine inlet area. *Answers: (a) -1.95 kJ/kg , (b) 10.2 MW , (c) 0.00447 m^2*

Problem (5-50C)

Assumptions 1 This is a steady-flow process since there is no change with time. 2 Potential energy changes are negligible. 3 The device is adiabatic and thus heat transfer is negligible.

Properties From the steam tables (Tables A-4 through 6)

$$\left. \begin{array}{l} P_1 = 10 \text{ MPa} \\ T_1 = 450^\circ\text{C} \end{array} \right\} \begin{array}{l} v_1 = 0.029782 \text{ m}^3/\text{kg} \\ h_1 = 3242.4 \text{ kJ/kg} \end{array}$$

and

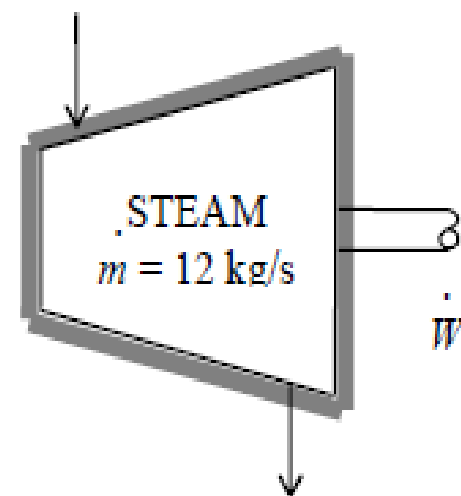
$$\left. \begin{array}{l} P_2 = 10 \text{ kPa} \\ x_2 = 0.92 \end{array} \right\} h_2 = h_f + x_2 h_{fg} = 191.81 + 0.92 \times 2392.1 = 2392.5 \text{ kJ/kg}$$

Analysis (a) The change in kinetic energy is determined from

$$\Delta ke = \frac{V_2^2 - V_1^2}{2} = \frac{(50 \text{ m/s})^2 - (80 \text{ m/s})^2}{2} \left(\frac{1 \text{ kJ/kg}}{1000 \text{ m}^2/\text{s}^2} \right) = -1.95 \text{ kJ/kg}$$

(b) There is only one inlet and one exit, and thus $\dot{m}_1 = \dot{m}_2 = \dot{m}$. We take the turbine as the system, which is a control volume since mass crosses the boundary. The energy balance for this steady-flow system can be expressed in the rate form as

$$\begin{array}{l} P_1 = 10 \text{ MPa} \\ T_1 = 450^\circ\text{C} \\ V_1 = 80 \text{ m/s} \end{array}$$



$$\begin{array}{l} P_2 = 10 \text{ kPa} \\ x_2 = 0.92 \\ V_2 = 50 \text{ m/s} \end{array}$$

Problem (5-50C)

$$\underbrace{\dot{E}_{\text{in}} - \dot{E}_{\text{out}}}_{\text{Rate of net energy transfer by heat, work, and mass}} = \underbrace{\Delta \dot{E}_{\text{system}}}_{\text{Rate of change in internal, kinetic, potential, etc. energies}} \stackrel{\approx 0 \text{ (steady)}}{=} 0$$

$$\dot{E}_{\text{in}} = \dot{E}_{\text{out}}$$

$$\dot{m}(h_1 + V_1^2 / 2) = \dot{W}_{\text{out}} + \dot{m}(h_2 + V_2^2 / 2) \quad (\text{since } \dot{Q} \cong \Delta \text{pe} \cong 0)$$

$$\dot{W}_{\text{out}} = -\dot{m} \left(h_2 - h_1 + \frac{V_2^2 - V_1^2}{2} \right)$$

Then the power output of the turbine is determined by substitution to be

$$\dot{W}_{\text{out}} = -(12 \text{ kg/s})(2392.5 - 3242.4 - 1.95) \text{ kJ/kg} = 10.2 \text{ MW}$$

(c) The inlet area of the turbine is determined from the mass flow rate relation,

$$\dot{m} = \frac{1}{\nu_1} A_1 V_1 \longrightarrow A_1 = \frac{\dot{m} \nu_1}{V_1} = \frac{(12 \text{ kg/s})(0.029782 \text{ m}^3/\text{kg})}{80 \text{ m/s}} = 0.00447 \text{ m}^2$$

Throttling Valves

$$h_2 \cong h_1$$

$$u_1 + P_1 v_1 = u_2 + P_2 v_2$$

Problem (5-61C)

During a throttling process, the temperature of a fluid drops from 30 to -20°C . Can this process occur adiabatically?

YES

Problem (5-62C)

5-64C Would you expect the temperature of air to drop as it undergoes a steady-flow throttling process? Explain.

5-62C No. Because air is an ideal gas and $h = h(T)$ for ideal gases. Thus if h remains constant, so does the temperature.

Problem (5-63C)

5-65C Would you expect the temperature of a liquid to change as it is throttled? Explain.

5-63C If it remains in the liquid phase, no. But if some of the liquid vaporizes during throttling, then yes.

Problem (5-67C)

5-67



Refrigerant-134a at 800 kPa and 25°C is throttled to a temperature of -20°C. Determine the pressure and the internal energy of the refrigerant at the final state. *Answers: 133 kPa, 80.7 kJ/kg*

5-67 Refrigerant-134a is throttled by a valve. The pressure and internal energy after expansion are to be determined.

Assumptions 1 This is a steady-flow process since there is no change with time. 2 Kinetic and potential energy changes are negligible. 3 Heat transfer to or from the fluid is negligible. 4 There are no work interactions involved.

Properties The inlet enthalpy of R-134a is, from the refrigerant tables (Tables A-11 through 13),

$$\left. \begin{array}{l} P_1 = 0.8 \text{ MPa} \\ T_1 = 25^\circ\text{C} \end{array} \right\} h_1 \cong h_{f@25^\circ\text{C}} = 86.41 \text{ kJ/kg}$$

Problem (5-67C)

Analysis There is only one inlet and one exit, and thus $\dot{m}_1 = \dot{m}_2 = \dot{m}$. We take the throttling valve as the system, which is a control volume since mass crosses the boundary. The energy balance for this steady-flow system can be expressed in the rate form as

$$\dot{E}_{\text{in}} - \dot{E}_{\text{out}} = \Delta \dot{E}_{\text{system}} \stackrel{\text{no (steady)}}{=} 0$$

$$\dot{E}_{\text{in}} = \dot{E}_{\text{out}}$$

$$\dot{m}h_1 = \dot{m}h_2$$

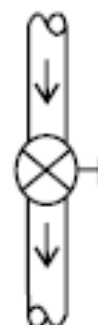
$$h_1 = h_2$$

since $\dot{Q} \cong \dot{W} = \Delta ke \cong \Delta pe \cong 0$. Then,

$$\left. \begin{array}{l} T_2 = -20^\circ\text{C} \\ (h_2 = h_1) \end{array} \right\} \begin{array}{l} h_f = 25.49 \text{ kJ/kg}, \quad u_f = 25.39 \text{ kJ/kg} \\ h_g = 238.41 \text{ kJ/kg}, \quad u_g = 218.84 \text{ kJ/kg} \end{array}$$

$$P_1 = 0.8 \text{ MPa}$$

$$T_1 = 25^\circ\text{C}$$



R-134a

$$T_2 = -20^\circ\text{C}$$

Obviously $h_f < h_2 < h_g$, thus the refrigerant exists as a saturated mixture at the exit state, and thus

$$P_2 = P_{\text{sat @ } -20^\circ\text{C}} = 132.82 \text{ kPa}$$

Also,

$$x_2 = \frac{h_2 - h_f}{h_{fg}} = \frac{86.41 - 25.49}{212.91} = 0.2861$$

Thus,

$$u_2 = u_f + x_2 u_{fg} = 25.39 + 0.2861 \times 193.45 = 80.74 \text{ kJ/kg}$$

Heat Exchanger

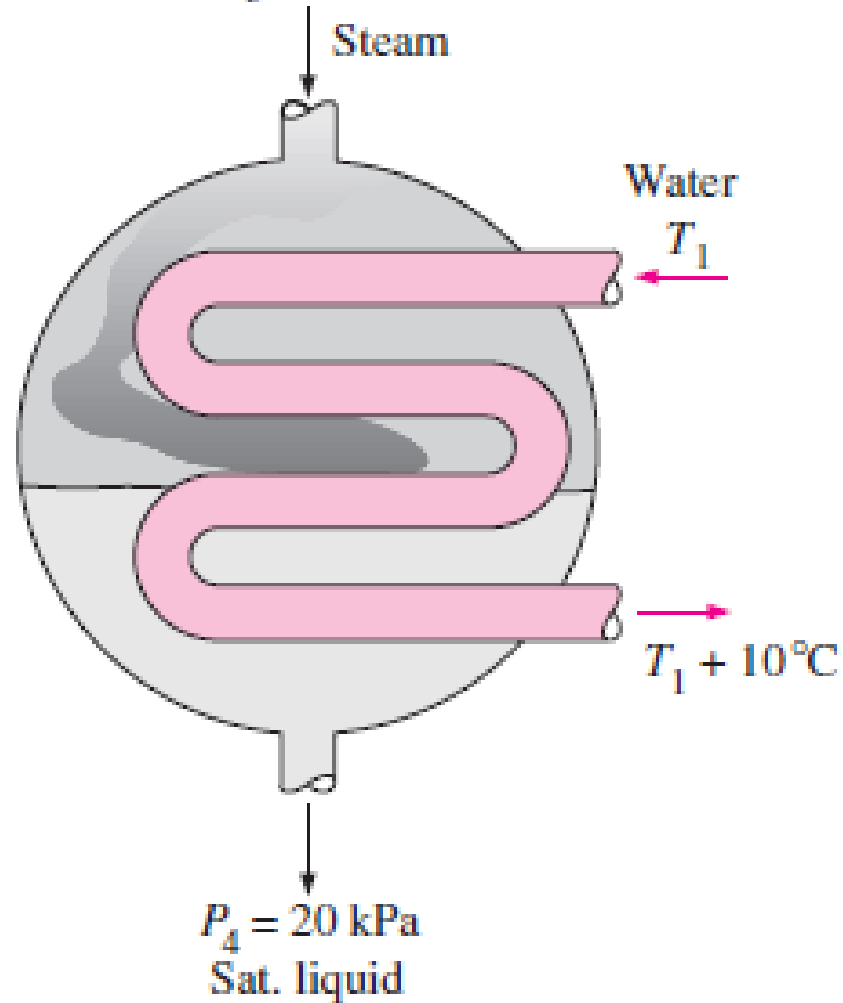
Problem (5-80C)

$$\dot{m}_3 = 20,000 \text{ kg/h}$$

$$P_3 = 20 \text{ kPa}$$

$$x_3 = 0.95$$

Steam



$$\dot{m}_{\text{Steam}} = 20000 \text{ kg/h}$$

$$\dot{m}_{\text{Water}} = ?$$

Problem (5-80C)

Assumptions 1 This is a steady-flow process since there is no change with time. 2 Kinetic and potential energy changes are negligible. 3 There are no work interactions. 4 Heat loss from the device to the surroundings is negligible and thus heat transfer from the hot fluid is equal to the heat transfer to the cold fluid. 5 Liquid water is an incompressible substance with constant specific heats at room temperature.

Properties The cooling water exists as compressed liquid at both states, and its specific heat at room temperature is $c = 4.18 \text{ kJ/kg}\cdot^\circ\text{C}$ (Table A-3). The enthalpies of the steam at the inlet and the exit states are (Tables A-5 and A-6)

$$\left. \begin{array}{l} P_3 = 20 \text{ kPa} \\ x_3 = 0.95 \end{array} \right\} h_3 = h_f + x_3 h_{fg} = 251.42 + 0.95 \times 2357.5 = 2491.1 \text{ kJ/kg}$$

$$\left. \begin{array}{l} P_4 = 20 \text{ kPa} \\ \text{sat. liquid} \end{array} \right\} h_4 \cong h_{f@20 \text{ kPa}} = 251.42 \text{ kJ/kg}$$

Analysis We take the heat exchanger as the system, which is a control volume. The mass and energy balances for this steady-flow system can be expressed in the rate form as

Problem (5-80C)

Mass balance (for each fluid stream):

$$\dot{m}_{in} - \dot{m}_{out} = \Delta \dot{m}_{system} \stackrel{\approx 0 \text{ (steady)}}{=} 0$$

$$\dot{m}_{in} = \dot{m}_{out}$$

$$\dot{m}_1 = \dot{m}_2 = \dot{m}_w \quad \text{and} \quad \dot{m}_3 = \dot{m}_4 = \dot{m}_s$$

Energy balance (for the heat exchanger):

$$\dot{E}_{in} - \dot{E}_{out} = \underbrace{\Delta \dot{E}_{system}}_{\approx 0 \text{ (steady)}} = 0$$

Rate of net energy transfer
by heat, work, and mass

Rate of change in internal, kinetic,
potential, etc. energies

$$\dot{E}_{in} = \dot{E}_{out}$$

$$\dot{m}_1 h_1 + \dot{m}_3 h_3 = \dot{m}_2 h_2 + \dot{m}_4 h_4 \quad (\text{since } \dot{Q} = \dot{W} = \Delta ke \approx \Delta pe \approx 0)$$

Combining the two,

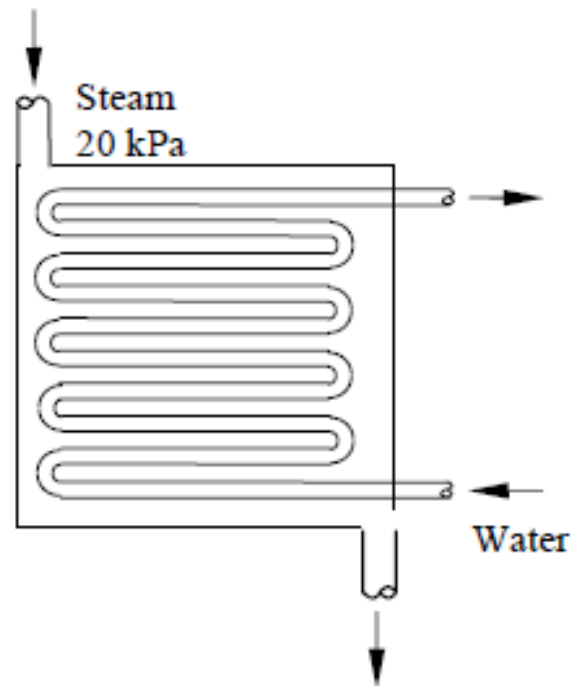
$$\dot{m}_w (h_2 - h_1) = \dot{m}_s (h_3 - h_4)$$

Solving for \dot{m}_w :

$$\dot{m}_w = \frac{h_3 - h_4}{h_2 - h_1} \dot{m}_s \approx \frac{h_3 - h_4}{c_p (T_2 - T_1)} \dot{m}_s$$

Substituting,

$$\dot{m}_w = \frac{(2491.1 - 251.42) \text{ kJ/kg}}{(4.18 \text{ kJ/kg} \cdot ^\circ \text{C})(10^\circ \text{C})} (20,000/3600 \text{ kg/s}) = \mathbf{297.7 \text{ kg/s}}$$

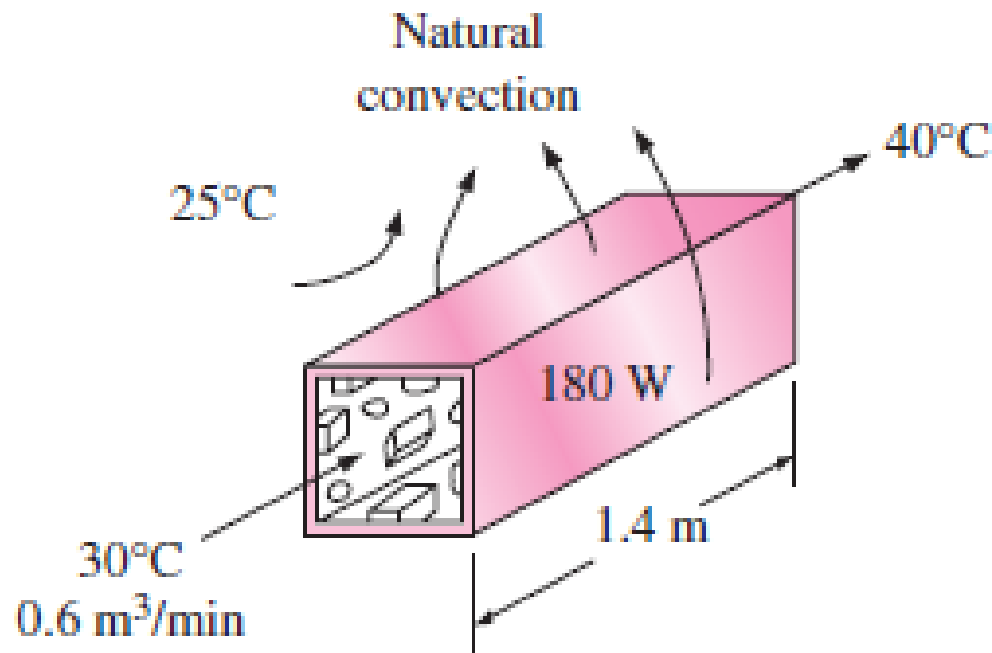


Pipe & Ducts

Problem (5-98C)



The components of an electronic system dissipating 180 W are located in a 1.4-m -long horizontal duct whose cross section is $20 \text{ cm} \times 20 \text{ cm}$. The components in the duct are cooled by forced air that enters the duct at 30°C and 1 atm at a rate of $0.6 \text{ m}^3/\text{min}$ and leaves at 40°C . Determine the rate of heat transfer from the outer surfaces of the duct to the ambient. *Answer: 63 W*



Problem (5-98C)

Assumptions 1 Steady operating conditions exist. 2 Air is an ideal gas with constant specific heats at room temperature. 3 Kinetic and potential energy changes are negligible

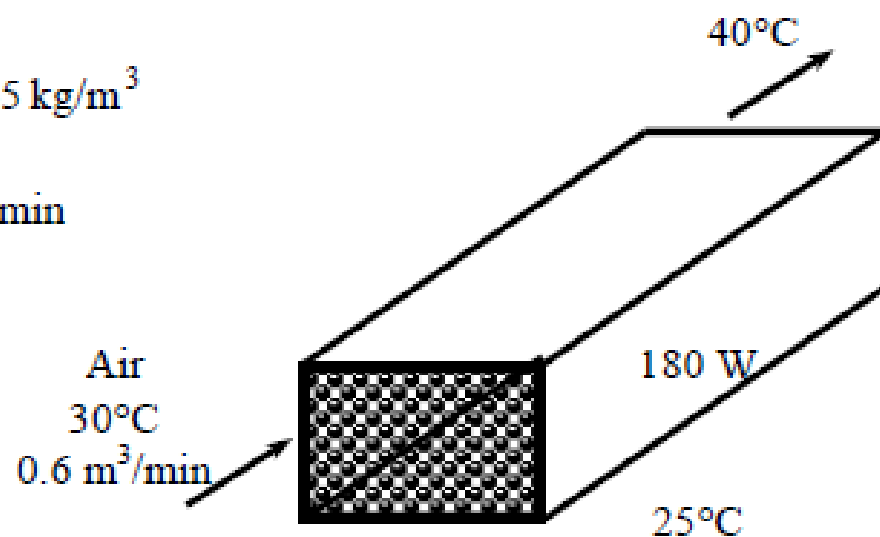
Properties The gas constant of air is $R = 0.287 \text{ kJ/kg}\cdot^\circ\text{C}$ (Table A-1). The specific heat of air at room temperature is $c_p = 1.005 \text{ kJ/kg}\cdot^\circ\text{C}$ (Table A-2).

Analysis The density of air entering the duct and the mass flow rate are

$$\rho = \frac{P}{RT} = \frac{101.325 \text{ kPa}}{(0.287 \text{ kPa}\cdot\text{m}^3/\text{kg}\cdot\text{K})(30 + 273)\text{K}} = 1.165 \text{ kg/m}^3$$

$$\dot{m} = \rho\dot{V} = (1.165 \text{ kg/m}^3)(0.6 \text{ m}^3/\text{min}) = 0.700 \text{ kg/min}$$

We take the channel, excluding the electronic components, to be the system, which is a control volume. The energy balance for this steady-flow system can be expressed in the rate form as



$$\underbrace{\dot{E}_{\text{in}} - \dot{E}_{\text{out}}}_{\text{Rate of net energy transfer by heat, work, and mass}} = \underbrace{\dot{\Delta E}_{\text{system}}}_{\text{Rate of change in internal, kinetic, potential, etc. energies}} \stackrel{\text{no (steady)}}{=} 0$$

Rate of net energy transfer by heat, work, and mass

Rate of change in internal, kinetic, potential, etc. energies

$$\dot{E}_{\text{in}} = \dot{E}_{\text{out}}$$

Problem (5-98C)

$$\dot{Q}_{\text{in}} + \dot{m}h_1 = \dot{m}h_2 \quad (\text{since } \Delta ke \cong \Delta pe \cong 0)$$

$$\dot{Q}_{\text{in}} = \dot{m}c_p(T_2 - T_1)$$

Then the rate of heat transfer to the air passing through the duct becomes

$$\dot{Q}_{\text{air}} = [\dot{m}c_p(T_{\text{out}} - T_{\text{in}})]_{\text{air}} = (0.700 / 60 \text{ kg/s})(1.005 \text{ kJ/kg} \cdot ^\circ\text{C})(40 - 30)^\circ\text{C} = 0.117 \text{ kW} = 117 \text{ W}$$

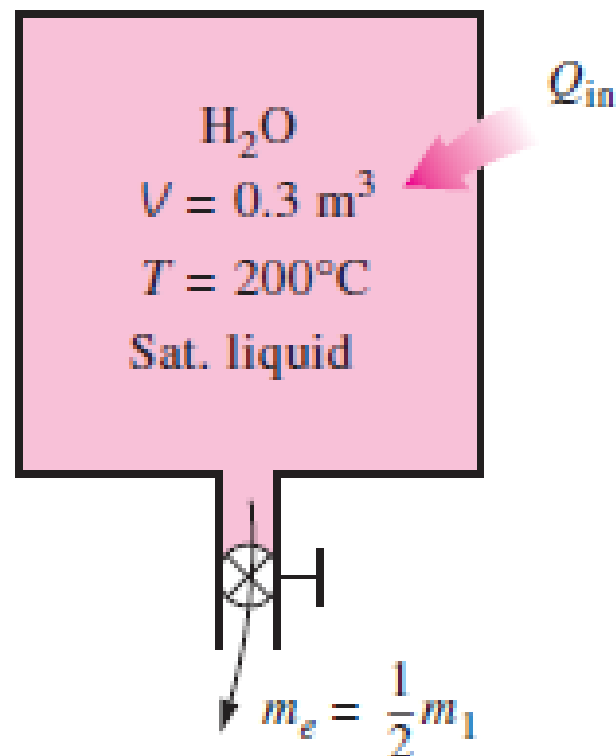
The rest of the 180 W heat generated must be dissipated through the outer surfaces of the duct by natural convection and radiation,

$$\dot{Q}_{\text{external}} = \dot{Q}_{\text{total}} - \dot{Q}_{\text{internal}} = 180 - 117 = 63 \text{ W}$$

Unsteady Flow Process

Problem (5-127C)

5-133 A 0.3-m^3 rigid tank is filled with saturated liquid water at 200°C . A valve at the bottom of the tank is opened, and liquid is withdrawn from the tank. Heat is transferred to the water such that the temperature in the tank remains constant. Determine the amount of heat that must be transferred by the time one-half of the total mass has been withdrawn.



Problem (5-127C)

Assumptions 1 This is an unsteady process since the conditions within the device are changing during the process, but it can be analyzed as a uniform-flow process since the state of fluid leaving the device remains constant. 2 Kinetic and potential energies are negligible. 3 There are no work interactions involved. 4 The direction of heat transfer is to the tank (will be verified).

Properties The properties of water are (Tables A-4 through A-6)

$$\left. \begin{array}{l} T_1 = 200^\circ\text{C} \\ \text{sat. liquid} \end{array} \right\} \begin{array}{l} v_1 = v_{f@200^\circ\text{C}} = 0.001157 \text{ m}^3/\text{kg} \\ u_1 = u_{f@200^\circ\text{C}} = 850.46 \text{ kJ/kg} \end{array}$$

$$\left. \begin{array}{l} T_e = 200^\circ\text{C} \\ \text{sat. liquid} \end{array} \right\} h_e = h_{f@200^\circ\text{C}} = 852.26 \text{ kJ/kg}$$

Problem (5-127C)

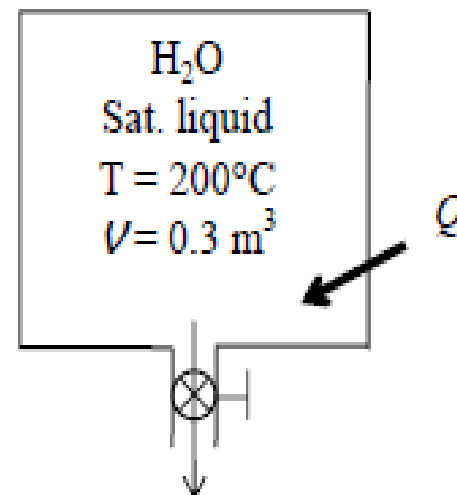
Analysis We take the tank as the system, which is a control volume since mass crosses the boundary. Noting that the microscopic energies of flowing and nonflowing fluids are represented by enthalpy h and internal energy u , respectively, the mass and energy balances for this uniform-flow system can be expressed as

Mass balance: $m_{\text{in}} - m_{\text{out}} = \Delta m_{\text{system}} \rightarrow m_e = m_1 - m_2$

Energy balance:

$$\underbrace{E_{\text{in}} - E_{\text{out}}}_{\substack{\text{Net energy transfer} \\ \text{by heat, work, and mass}}} = \underbrace{\Delta E_{\text{system}}}_{\substack{\text{Change in internal, kinetic,} \\ \text{potential, etc. energies}}}$$

$$Q_{\text{in}} = m_e h_e + m_2 u_2 - m_1 u_1 \quad (\text{since } W \cong ke \cong pe \cong 0)$$



The initial and the final masses in the tank are

Problem (5-127C)

The initial and the final masses in the tank are

$$m_1 = \frac{V_1}{v_1} = \frac{0.3 \text{ m}^3}{0.001157 \text{ m}^3/\text{kg}} = 259.4 \text{ kg}$$

$$m_2 = \frac{1}{2} m_1 = \frac{1}{2} (259.4 \text{ kg}) = 129.7 \text{ kg}$$

Then from the mass balance,

$$m_e = m_1 - m_2 = 259.4 - 129.7 = 129.7 \text{ kg}$$

Now we determine the final internal energy,

$$v_2 = \frac{V}{m_2} = \frac{0.3 \text{ m}^3}{129.7 \text{ kg}} = 0.002313 \text{ m}^3/\text{kg}$$

$$x_2 = \frac{v_2 - v_f}{v_{fg}} = \frac{0.002313 - 0.001157}{0.12721 - 0.001157} = 0.009171$$

$$\left. \begin{array}{l} T_2 = 200^\circ\text{C} \\ x_2 = 0.009171 \end{array} \right\} u_2 = u_f + x_2 u_{fg} = 850.46 + (0.009171)(1743.7) = 866.46 \text{ kJ/kg}$$

Then the heat transfer during this process is determined from the energy balance by substitution to be

$$\begin{aligned} Q &= (129.7 \text{ kg})(852.26 \text{ kJ/kg}) + (129.7 \text{ kg})(866.46 \text{ kJ/kg}) - (259.4 \text{ kg})(850.46 \text{ kJ/kg}) \\ &= 2308 \text{ kJ} \end{aligned}$$

THE END